

## **Abstract**

The classification of the local Galois representations using  $(\phi, \Gamma)$ -modules by Fontaine has been generalized by Kisin and Ren over the Lubin-Tate extensions of local fields using the theory of  $(\phi, \psi; LT)$ -modules. In this thesis, we extend the work of (Fontaine) Herr by introducing a complex which allows us to compute cohomology over the Lubin-Tate extensions and compare it with the Galois cohomology groups. We further extend that complex to include certain non-abelian extensions. We then deduce some relations of this cohomology with those arising from  $(\psi, \phi; LT)$ -modules. We also compute the Iwasawa cohomology over the Lubin-Tate extensions in terms of  $\psi$ -operator acting on étale  $(\phi, \psi; LT)$ -module attached to the local Galois representation. Moreover, we generalize the notion of  $(\phi, \psi; LT)$ -modules over the coefficient ring  $R$  and show that the equivalence given by Kisin and Ren extends to the Galois representations over  $R$ . This equivalence allows us to generalize our results to the case of coefficient rings.