In this thesis, I have discussed different types of operators and their indices. Begin- ning with basics of compact operators and their properties, I gave an exposition on Fredholm operators between Banach spaces. I have also shown that compact oper- ators are the furthest from Fredholm operators in infinite dimensional space. And finally, I studied Toeplitz operators which are Fredholm operators with an invertible symbol.